

Name: \_\_\_\_\_

Section: \_\_\_\_\_

**Important:** For all three problems, let

$$A = \begin{bmatrix} -2 & -3 & 0 \\ 0 & 0 & 0 \\ 4 & 7 & 2 \end{bmatrix}$$

1. Find the eigenvalues of  $A$  and a basis for each eigenspace.

2. Find a matrix  $P$  such that  $P^{-1}AP$  is diagonal.

3. Explain in a few words why you could have computed at least one of the eigenvalues of  $A$  without using the characteristic polynomial.